# CS4641 Machine Learning - Homework 3

## Bo Dai

# Deadline: 03/24 Mon, 23:59 PM

- Submit your answers as 1) one single PDF file to *HW3* and 2) one Jupyter Notebook file to *HW3\_code* on Gradescope. **IMPORTANT:** The solution to each problem/subproblem must be on a separate page. When submitting to Gradescope, please make sure to mark the page(s) corresponding to each problem/subproblem.
- You will be allowed 2 total late days (48 hours) without penalty for the entire semester. Once those days are used, you will be penalized according to the following policy:
  - Homework is worth full credit before the due time.
  - It is worth 75% credit for the next 24 hours.
  - It is worth 50% credit for the second 24 hours.
  - It is worth zero credit after that.
- You are required to use Latex, or word processing software, to generate your solutions to the written questions. Handwritten solutions WILL NOT BE ACCEPTED.

#### 1 Naive Bayes

Please submit the solution to this problem to HW3 on Gradescope.

In medical diagnosis, doctors often need to determine whether a patient has a certain disease based on symptoms. Suppose a hospital research team has collected historical patient data with three key binary features: **Hypertension**  $(X_1)$ , **High Cholesterol**  $(X_2)$ , and **Family History**  $(X_3)$ , along with the diagnosis result (Y) indicating whether the patient has the disease.

In this problem, we assume that the features  $X_1, X_2, X_3$  are conditionally independent given Y. The dataset is given as follows:

Patient ID	Hypertension $(X_1)$	High Cholesterol $(X_2)$	Family History $(X_3)$	Disease $(Y)$
1	1	1	1	1
2	1	0	1	1
3	0	1	0	0
4	1	1	0	0
5	0	0	1	0
6	1	0	0	0
7	0	1	0	1
8	0	0	1	0

A patient is considered to have the disease (Y = 1) if they exhibit symptoms matching past cases where the disease was diagnosed, and they are considered healthy (Y = 0) otherwise.

Using the dataset above, answer the following questions:

- [15 points] Compute the prior probabilities of having the disease and being healthy.
- [15 points] Compute the conditional probabilities of each symptom given the disease status. That is, calculate  $P(X_j = 1 | Y = 1)$  and  $P(X_j = 1 | Y = 0)$  for each j = 1, 2, 3 corresponding to Hypertension, High Cholesterol, and Family History.
- [20 points] A new patient arrives at the hospital with the following symptoms: having hypertension, not having high cholesterol, and having a family history of the disease. Using Bernoulli Naive Bayes, compute the posterior probabilities of this patient having the disease  $(P(Y = 1 | X_1 = 1, X_2 = 0, X_3 = 1))$  and being healthy  $(P(Y = 0 | X_1 = 1, X_2 = 0, X_3 = 1))$ .

# 2 K-means

Please submit the completed notebook to  $HW3\_code$  on Gradescope.

# 2.1 Description

For this problem, you will implement the K-means algorithm using the Numpy library. Concretely, you need to complete the TODOs in the following .ipynb file.

https://drive.google.com/file/d/1dpxpet2-CdGT4v-8krH9o1ddp9vciXXa/view?usp=sharing

# 2.2 Implementation TODOs

#### 1. Setup

• No implementation required (code provided)

#### 2. Helper Function Implementation[30 points]

- euclidean\_distance(): 5 points
- initialize\_centroids(): 5 points
- assign\_clusters(): 10 points
- update\_centroids(): 10 points

#### 3. K-means Algorithm Implementation [20 points]

• Implement the main k\_means() function using your helper functions

#### 4. Comparison with scikit-learn Implementation

• No implementation required (code provided)

#### 5. Elbow Method Analysis

• No implementation required (code provided)

### 2.3 Implementation and Submission Rules

- You can either download the notebook and complete the TODOs in your local environment, or make a copy and modify it on Google Colab.
- Use only Numpy for your implementation (no scikit-learn/scipy for clustering functions)
- Please submit your completed .ipynb file including all the outputs of each block to HW3\_code on Gradescope.